

**Charge dispersion MPGD Readout & ILC-TPC  
Prototype Test Beam Studies**

**Madhu Dixit  
Carleton University & TRIUMF**

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## Motivation & overview

- ILC tracker goal  $\Delta(1/p_T) \leq 5 \cdot 10^{-5} \text{ (GeV/c)}^{-1}$   
=> MPGD-TPC  $\Delta(1/p_T) \leq 1.5 \times 10^{-4} \text{ (GeV/c)}^{-1}$
- TDR TPC: 200 pads;  $\sigma_{Tr} \sim 100 \text{ } \mu\text{m}$  ( $\approx 2 \text{ m drift}$ ), pad size  $2 \times 6 \text{ mm}^2$   
=> Total TPC pad count  $\sim 1.5 \times 10^6$
- R&D shows 2 mm too wide for  $100 \text{ } \mu\text{m}$  resolution with normal readout.  
Ways to improve the MPGD-TPC resolution:
  - 1) Under consideration - narrower 1 mm x 6 mm pads ( $3 \times 10^6$  total). R&D issues: High density electronics, increased heat load, TPC endcap mass etc.
  - 2) Alternative: Disperse avalanche charge to improve resolution for wide pads. Development of TPC readout with charge dispersion in MPGDs with a resistive anode.
    - Charge dispersion demonstrated in cosmic ray TPC tests with no magnet.
    - The new TPC readout concept was tested in a beam test last October. 1 T superconducting magnet & 4 GeV/c hadron test beam at KEK PS.
    - Two TPCs: Multi Technology Test TPC - MT3 TPC (MPI Munich) + Carleton TPC with Micromegas (Saclay) & GEMs(Saga University).
    - Two weeks of beam data in October 2005.
  - 3) Magnetic field performance of MPGD-TPC with charge dispersion readout in a test beam.

## Diffusion sets the limit on TPC momentum resolution

- The physics limit of TPC resolution comes from transverse diffusion:

$$\sigma_x^2 \approx \frac{D_{Tr}^2 \cdot z}{N_{eff}} \quad N_{eff} = \text{effective electron statistics.}$$

- For best resolution, choose a gas with smallest diffusion

The rule applies to the wire TPCs which use induced cathode pad signals for position determination. But **ExB** & track angle systematic effects degrade wire TPC resolution.

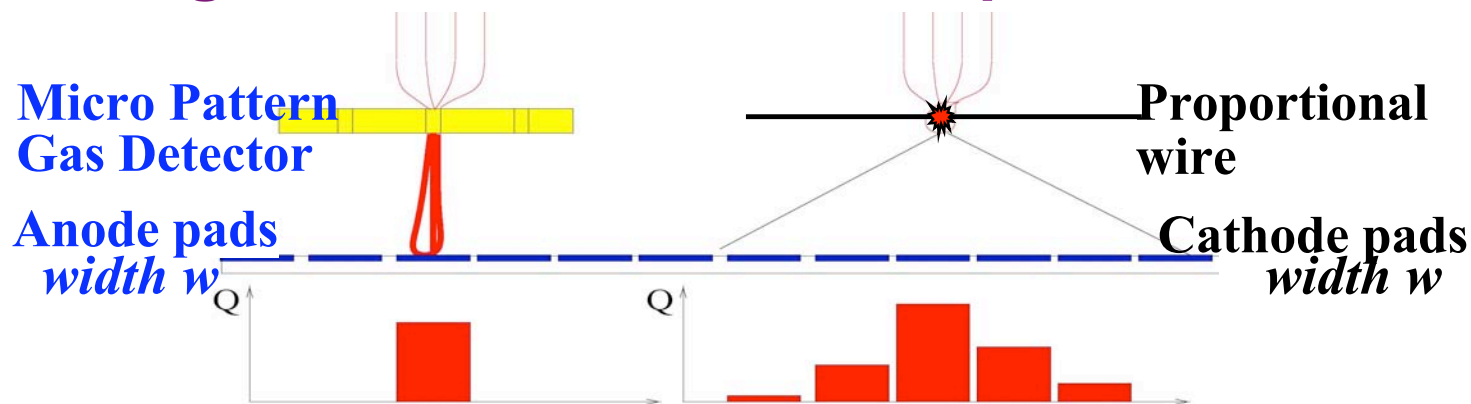
**ExB** effect does not limit the MPGD-TPC. But there are no comparable induced cathode pad signals.

The MPGD-TPC resolution is limited by pad width  $w$ . The resolution gets worse for wide pads in absence of diffusion.

$$\sigma_x^2 \Rightarrow \frac{w^2}{12} \quad \text{as } z \Rightarrow 0$$

# Pad width limits the MPGD-TPC resolution

## ExB angle effects limit the wire/pad TPC resolution



**Direct signal on the MPGD anode pad**  
 For small diffusion, less precise centroid for wide pads

**Induced cathode signal determined by geometry**  
 Accurate centroid determination possible with wide pads

$$\sigma_x^2 \approx \sigma_0^2 + \frac{1}{N_{eff}} \left[ D_{Tr}^2 z + w^2 / 12 \right]$$

$$\sigma_x^2 \approx \sigma_0^2 + \frac{D_{Tr}^2 \cdot z}{N_{eff}}$$

## Improving MPGD TPC resolution without resorting to narrower pads

- Disperse track charge after gas gain to improve centroid determination with wide pads.
- For the GEM, large transverse diffusion in the high E-field field in transfer and induction gaps provides a natural mechanism to disperse the cluster charge.
- Measurements with prototype GEM-TPCs indicate that  $\sim 1$  mm wide pads may be needed for TPC operation in high magnetic fields.
- Explore other concepts to disperse the charge

Charge dispersion - a geometrical pad signal induction mechanism making position sensing insensitive to pad width.

# Position sensing from charge dispersion in a MPGD with a resistive anode

Position sensing on a resistive anode proportional wire from charge division

Telegraph equation (1-D):

$$\frac{L}{R} \frac{\partial^2 Q}{\partial t^2} + \frac{\partial Q}{\partial t} = \frac{1}{RC} \frac{\partial^2 Q}{\partial x^2}$$

Deposit point charge at  $t=0$

Solution for charge density ( $L \sim 0$ )

$$Q(x,t) = \sqrt{\frac{RC}{4\pi t}} e^{-\frac{x^2 RC}{4t}}$$

Generalize charge division on a resistive wire to 2 D

## Position sensing from charge dispersion in MPGDs with a resistive anode

Equivalent to Telegraph equation in 2-D

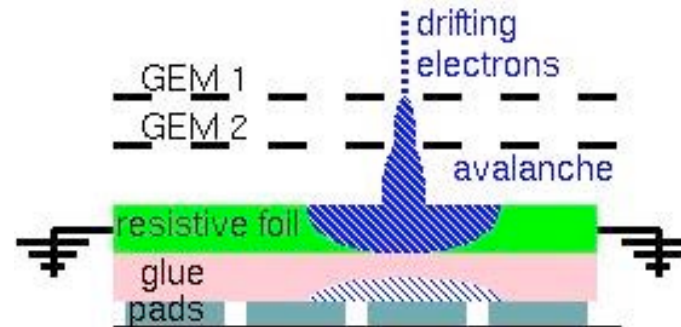
$$\frac{\partial Q}{\partial t} = \frac{1}{RC} \left[ \frac{\partial^2 Q}{\partial r^2} + \frac{1}{r} \frac{\partial Q}{\partial r} \right]$$

Solution for charge density in 2-D

$$Q(r,t) = \frac{RC}{2t} e^{-\frac{r^2 RC}{4t}}$$

# Charge dispersion in a MPGD with a resistive anode

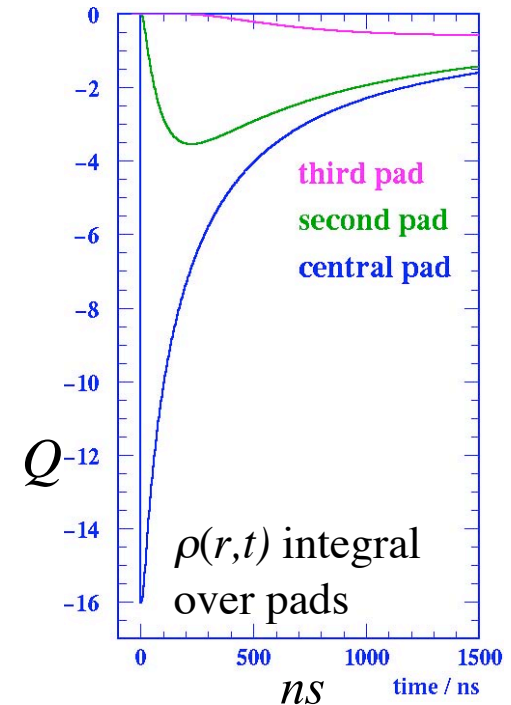
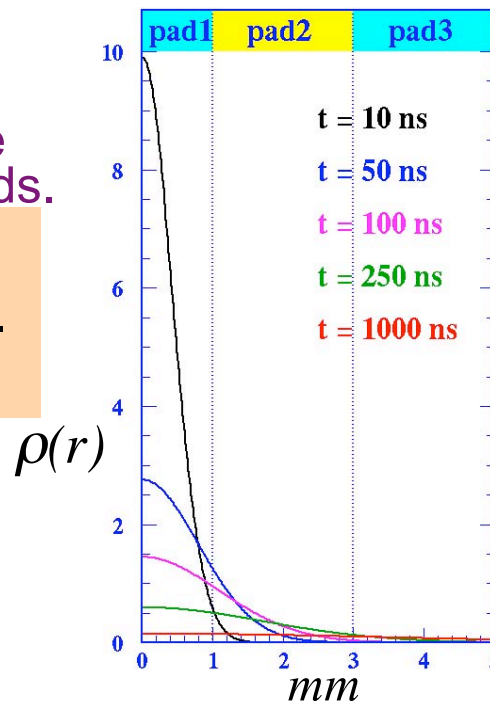
- Modified MPGD anode with a high resistivity film bonded to a readout plane with an insulating spacer.
- 2-dimensional continuous RC network defined by material properties & geometry.
- Point charge at  $r = 0$  &  $t = 0$  disperses with time.
- Time dependent anode charge density sampled by readout pads.



Equation for surface charge density function on the 2-dim. continuous RC network:

$$\frac{\partial \rho}{\partial t} = \frac{1}{RC} \left[ \frac{\partial^2 \rho}{\partial r^2} + \frac{1}{r} \frac{\partial \rho}{\partial r} \right]$$

$$\Rightarrow \rho(r, t) = \frac{RC}{2t} e^{-\frac{r^2 RC}{4t}}$$



*M.S.Dixit et.al., Nucl. Instrum. Methods A518 (2004) 721.*

## Simulation of charge dispersion phenomenon

- The charge dispersion equation describes the time evolution of a point like charge deposited on the MPGD resistive anode at  $t = 0$ .
- To compare to experiment, one needs to include the effects of:
  - Longitudinal & transverse diffusion in the gas.
  - Intrinsic rise time  $T_{rise}$  of the detector charge pulse.
  - The effect of preamplifier rise and fall times  $t_r$  &  $t_f$ .
  - And for particle tracks, the effects of primary ionization clustering.



## The simulation for a single charge cluster

The charge density function for a point charge in Cartesian coordinates:

$$\rho_{\delta}(x, y, t) = \frac{\tau}{4\pi t} \exp\left[-\tau(x^2 + y^2)/4t\right] \text{ where } \tau = RC$$

Physics effects included in simulation in two parts: 1) as effects which depend on spatial coordinates  $x$  &  $y$ , or; 2) as effects which depend on time.

1) The spatial effects function includes charge dispersion phenomena & transverse size  $w$  of the charge cluster due to transverse diffusion.

$Q_{pad}(t)$  is the pad signal from charge dispersion when a charge  $Nq_e$  of size  $w$  is deposited on the anode at  $t = 0$ ;

$$Q_{pad} = \frac{Nq_e}{4} \left[ \operatorname{erf}\left(\frac{x_{high}}{\sqrt{2}\sigma_{xy}}\right) - \operatorname{erf}\left(\frac{x_{low}}{\sqrt{2}\sigma_{xy}}\right) \right] \left[ \operatorname{erf}\left(\frac{y_{high}}{\sqrt{2}\sigma_{xy}}\right) - \operatorname{erf}\left(\frac{y_{low}}{\sqrt{2}\sigma_{xy}}\right) \right] \quad (1)$$

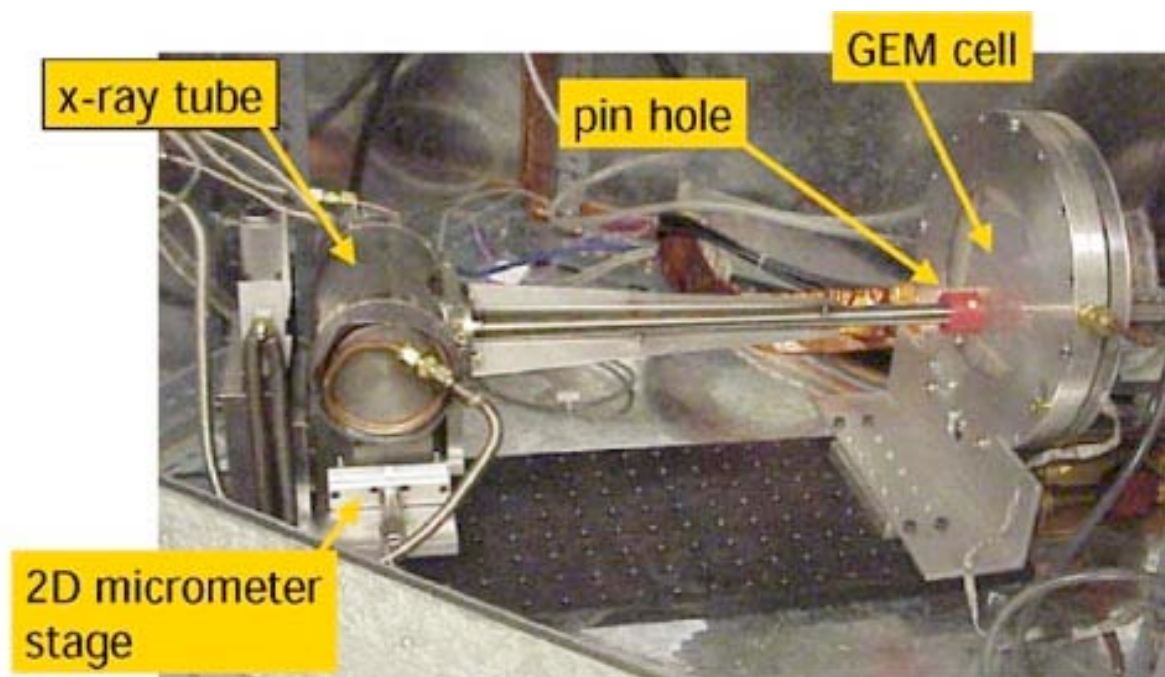
$x_{high}$ ,  $x_{low}$ ,  $y_{high}$ ,  $y_{low}$  define the pad boundaries &  $\sigma_{xy} = \sqrt{2t/\tau + w^2}$

$$I(t) = \frac{1}{2T_{rise}} \left[ \begin{aligned} & \exp(\sigma^2 a^2 / 2 - at) \left[ \operatorname{erf} \left( \frac{t - T_{rise} - \sigma^2 a}{\sigma \sqrt{2}} \right) + 1 \right] - \\ & \exp(\sigma^2 b^2 / 2 - bt) \left[ \operatorname{erf} \left( \frac{t - T_{rise} - \sigma^2 b}{\sigma \sqrt{2}} \right) + 1 \right] + \\ & \exp(\sigma^2 a^2 / 2 - a(t - T_{rise})) \left[ \operatorname{erf} \left( \frac{t - 2T_{rise} - \sigma^2 a}{\sigma \sqrt{2}} \right) + 1 \right] - \\ & \exp(\sigma^2 b^2 / 2 - b(t - T_{rise})) \left[ \operatorname{erf} \left( \frac{t - 2T_{rise} - \sigma^2 b}{\sigma \sqrt{2}} \right) + 1 \right] + \\ & \exp(\sigma^2 a^2 / 2 - at) \left[ \operatorname{erf} \left( \frac{t - \sigma^2 a}{\sigma \sqrt{2}} \right) + \operatorname{erf} \left( \frac{t - T_{rise} - \sigma^2 a}{\sigma \sqrt{2}} \right) \right] - \\ & \exp(\sigma^2 b^2 / 2 - bt) \left[ \operatorname{erf} \left( \frac{t - \sigma^2 b}{\sigma \sqrt{2}} \right) + \operatorname{erf} \left( \frac{t - T_{rise} - \sigma^2 b}{\sigma \sqrt{2}} \right) \right] \end{aligned} \right] \quad (2)$$

$I(t)$  incorporates intrinsic rise time, longitudinal diffusion & electronics shaping times as time dependent effects.  $a = 1/t_f$ ;  $b = 1/t_f + 1/t_r$

(1) and (2) are convoluted numerically for the model simulation.

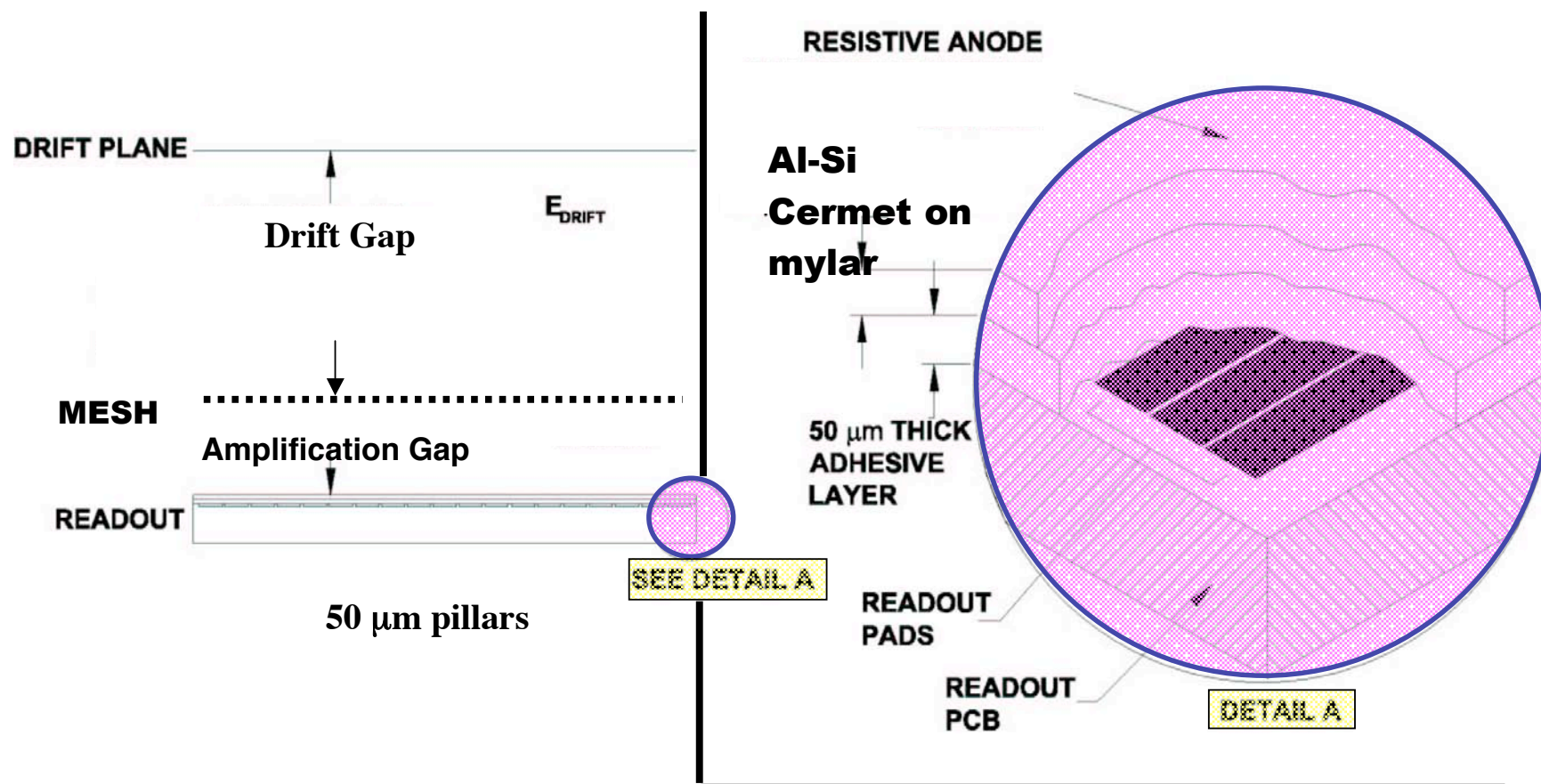
## MPGD charge dispersion tests with a collimated point x ray source



- Point source  $\sim 50 \mu\text{m}$  collimated 4.5 keV x rays.
- Aleph TPC preamps.  $\tau_{\text{Rise}} = 40 \text{ ns}$ ,  $\tau_{\text{Fall}} = 2 \mu\text{s}$ .
- DAQ - 500 MHz Tektronix digital scope.

## Resistive anode Micromegas

530 k $\Omega$ /□ Carbon loaded Kapton resistive anode was used with GEM. This was replaced with higher resistivity 1 M $\Omega$ /□ Cermet for tests with Micromegas.

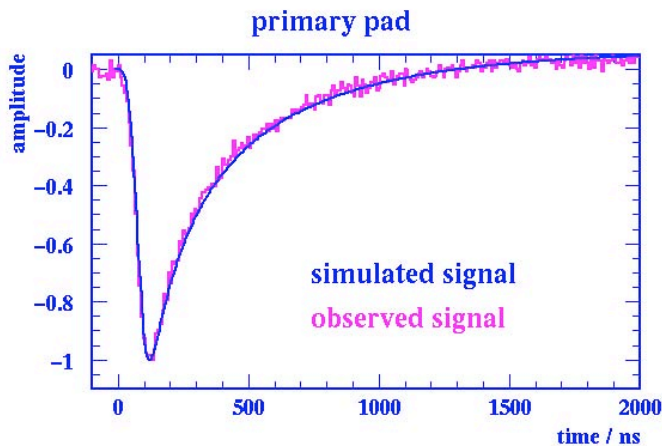


# Charge dispersion signal for a GEM

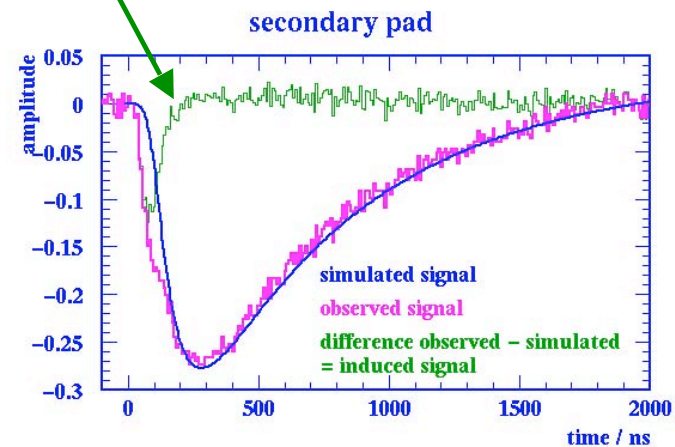
## Simulation versus measurement (Ar+10%CO<sub>2</sub>)

(2 x 6 mm<sup>2</sup> pads) Collimated ~ 50 μm 4.5 keV x-ray spot on pad centre.

Difference = induced signal (not included in simulation) studied previously: MPGD '99 (Orsay), LCWS '00



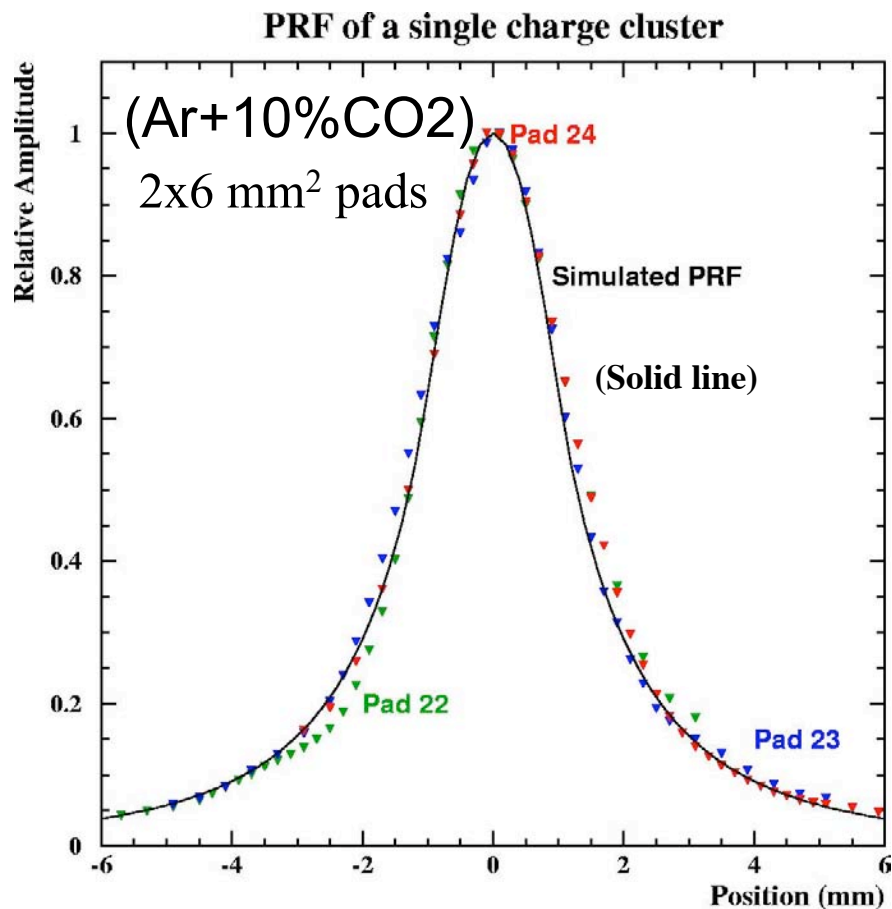
Simulated primary pulse is normalized to the data.



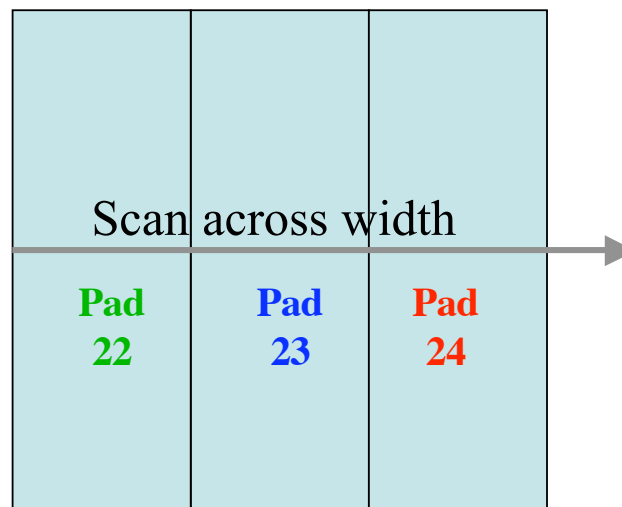
Primary pulse normalization used for the simulated secondary pulse

# GEM pad response function (PRF) for a point source

## Simulation compared to the measured PRF



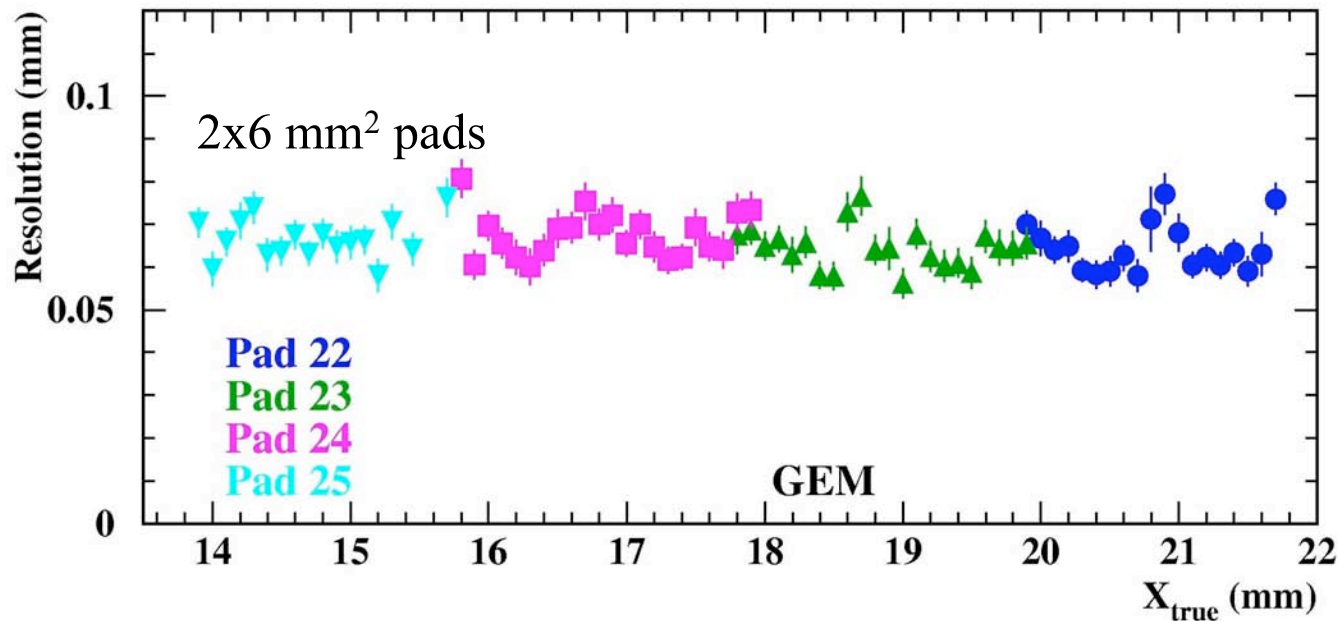
Ionization from 50  $\mu\text{m}$  collimated x-ray spot.



Measured PRF deviates from simulation due to anode RC nonuniformities.

PRF - a measure of signal amplitude as a function of cluster position.

**Double-GEM space point resolution with  
charge dispersion readout (Ar+10%CO<sub>2</sub>)  
Collimated ~ 4.5 keV x rays, Spot size ~ 50  $\mu\text{m}$**

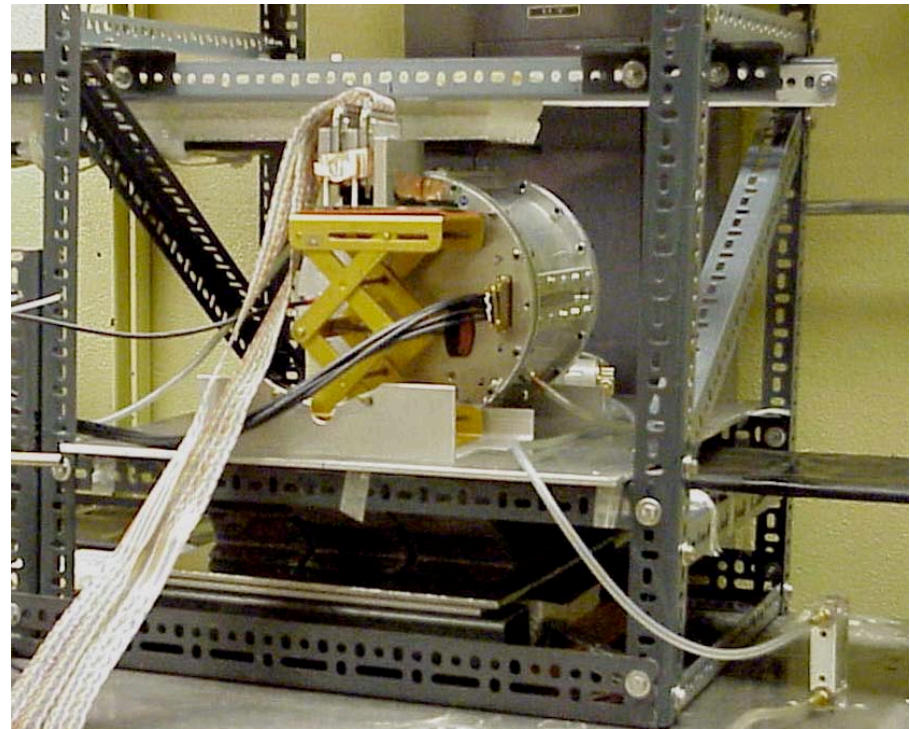


- GEM resolution ~ 70  $\mu\text{m}$ .
- Similar resolution measured for a Micromegas with a resistive anode readout using 2 mm x 6 mm pads

# Cosmic ray TPC tests with charge dispersion

- 15 cm drift length with GEM or Micromegas readout
- $B=0$
- Ar+10% CO<sub>2</sub> chosen to simulate low transverse diffusion in a magnetic field.
- Aleph charge preamps.  
 $\tau_{\text{Rise}} = 40 \text{ ns}$ ,  $\tau_{\text{Fall}} = 2 \mu\text{s}$ .
- 200 MHz FADCs rebinned to digitization effectively at 25 MHz.
- 60 tracking pads ( $2 \times 6 \text{ mm}^2$ )  
+ 2 trigger pads ( $24 \times 6 \text{ mm}^2$ ).

The GEM-TPC resolution was first measured with conventional direct charge TPC readout.

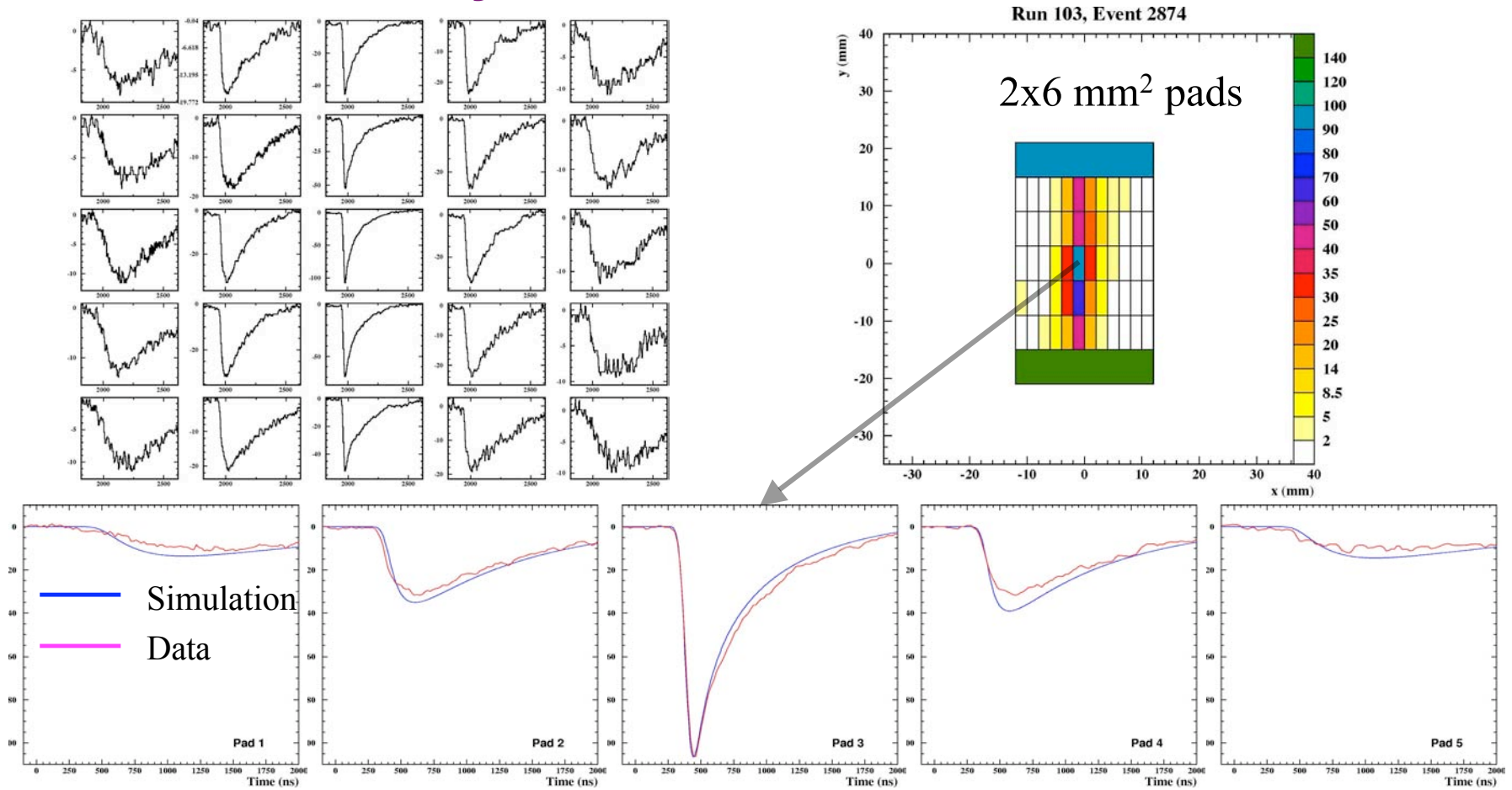


The resolution was next measured with a charge dispersion resistive anode readout with a double-GEM & with a Micromegas endcap.



# GEM TPC charge dispersion simulation (B=0)

## Cosmic ray track, Z = 67 mm Ar+10%CO<sub>2</sub>



Centre pulse used for simulation normalization - no other free parameters.

## The pad response function (PRF) for a track

- The PRF is a measure of signal size as a function of track position relative to the pad.
- Unusual highly variable charge dispersion pulse shape; both the rise time & pulse amplitude depend on track position.
- We use pulse shape information to optimize the PRF.
- The PRF can, in principle, be determined from simulation.
- However, system RC nonuniformities & geometrical effects introduce bias in absolute position determination.
- The position bias can be corrected by calibration.
- PRF and bias determined empirically using a subset of data which was used for calibration. The remaining data used for resolution studies.

## Track PRFs with GEM & Micromegas readout

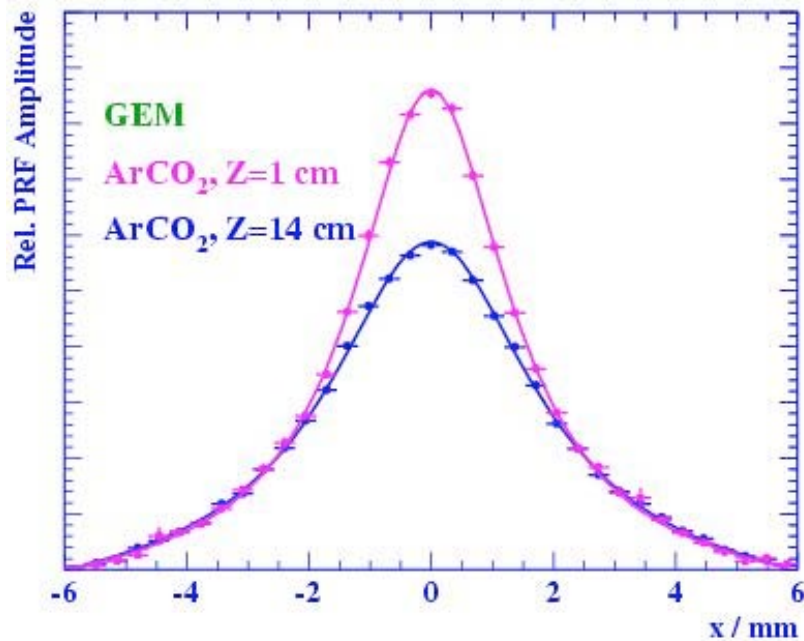
- The PRFs are not Gaussian.
- The PRF depends on track position relative to the pad.
- $PRF = PRF(x,z)$
- PRF can be characterized by its FWHM  $\Gamma(z)$  & base width  $\Delta(z)$ .
- PRFs determined from the data have been fitted to a functional form consisting of a ratio of two symmetric 4th order polynomials.

$$PRF[x, \Gamma(z), \Delta, a, b] = \frac{(1 + a_2 x^2 + a_4 x^4)}{(1 + b_2 x^2 + b_4 x^4)}$$

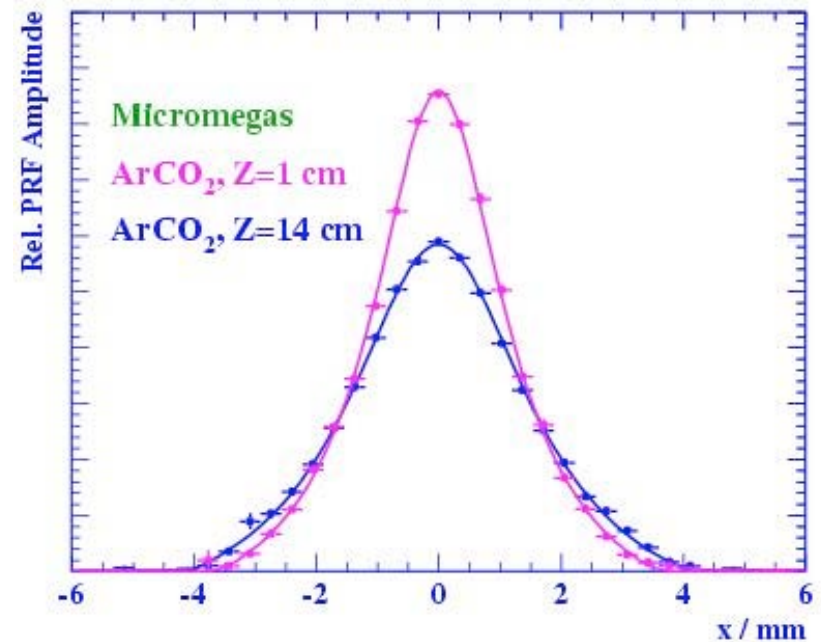
$a_2$   $a_4$   $b_2$  &  $b_4$  can be written down in terms of  $\Gamma$  and  $\Delta$  & two scale parameters  $a$  &  $b$ .

## GEM & Micromegas PRFs for tracks Ar+10%CO<sub>2</sub> 2x6 mm<sup>2</sup> pads

The pad response function amplitude for longer drift distances is lower due to Z dependent normalization.



GEM PRFs



Micromegas PRFs

Micromegas PRF is narrower due to the use of higher resistivity anode & smaller diffusion than GEM after avalanche gain

## Track fit using the the PRF

Track at:  $x_{track} = x_0 + \tan(\phi) y_{row}$

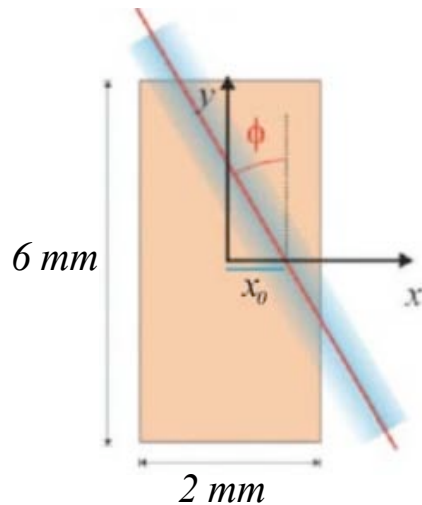
$$\chi^2 = \sum_{\text{rows}} \sum_{\text{i=pads}} [(A_i - PRF_i) / \partial A_i]^2$$

Determine  $x_0$  &  $\phi$  by minimizing  $\chi^2$  for the entire event

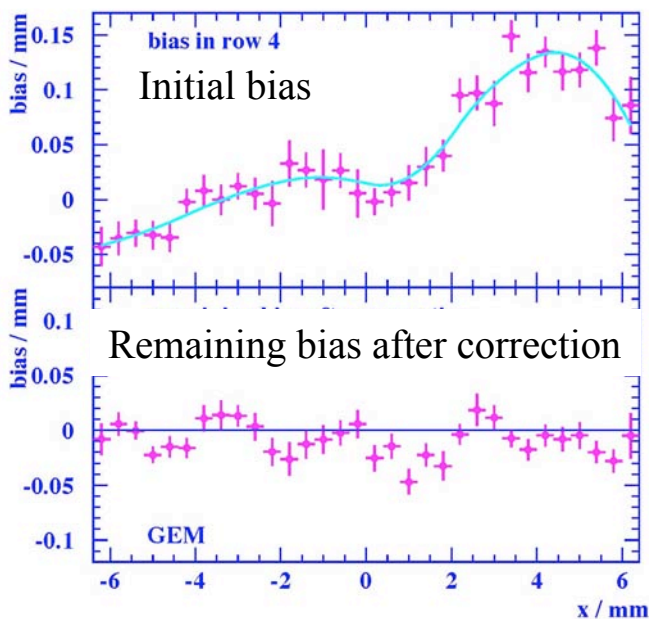
One parameter fit for  $x_{row}$  (track position for a given row) using  $\phi$

Bias = Mean of residuals ( $x_{row} - x_{track}$ ) as a function of  $x_{track}$

Resolution =  $\sigma$  of track residuals for tracks with  $|\phi| < 5^\circ$

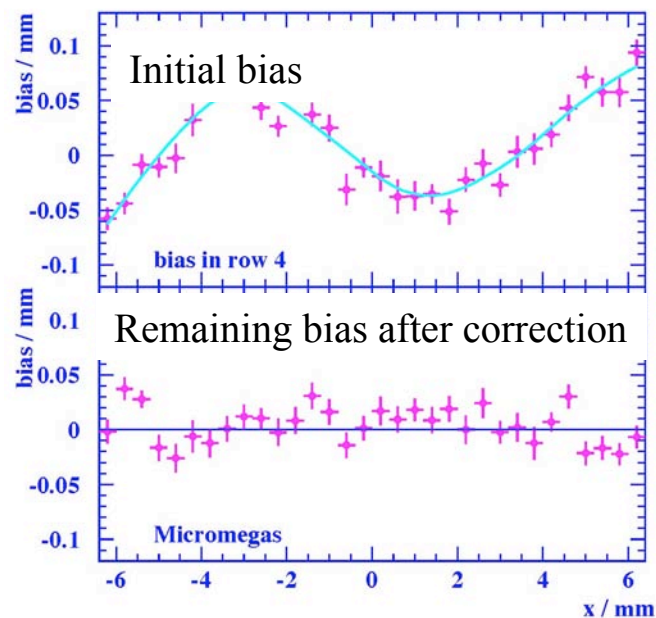


# Bias corrections for the GEM & for Micromegas



2x6 mm<sup>2</sup> pads

**GEM**



2x6 mm<sup>2</sup> pads

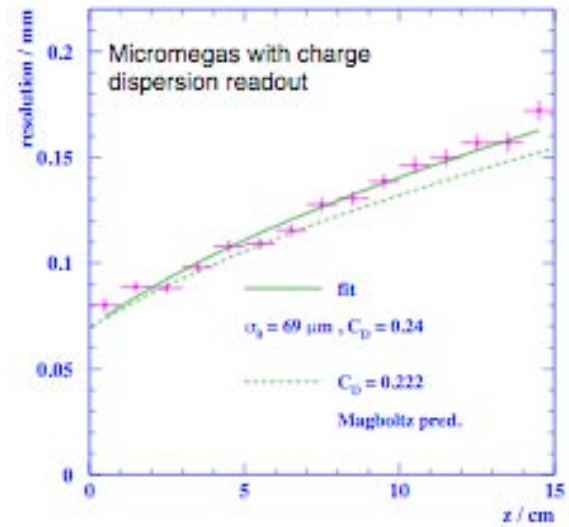
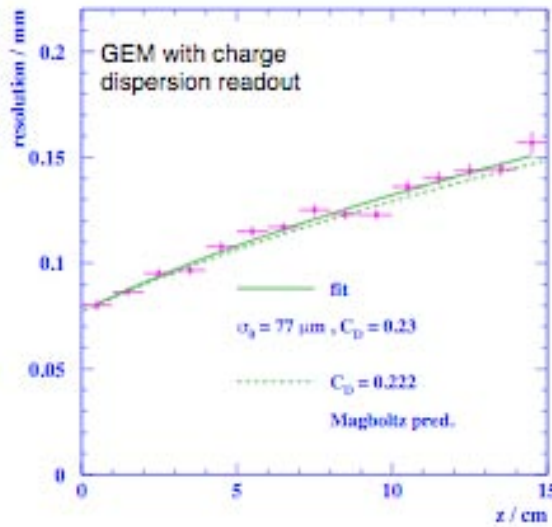
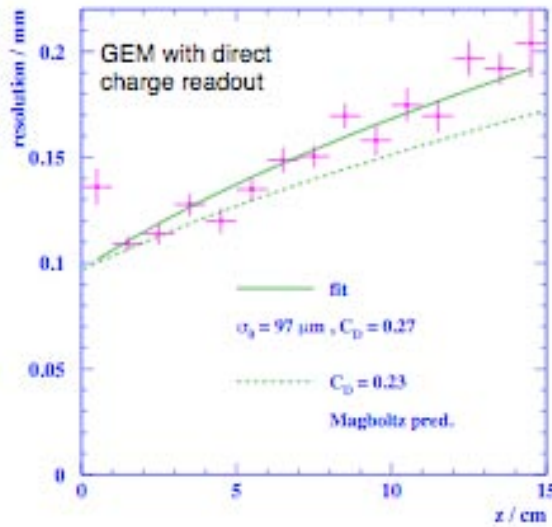
**Micromegas**

# Transverse resolution for cosmic rays Ar+10%CO2 (B=0)

R.K.Carnegie et.al.,  
NIM A538 (2005) 372

R.K.Carnegie et.al.,  
to be published

To be published



.....  $\sqrt{\sigma_0^2 + \frac{C_D^2}{N_e} z}$

Compared to conventional readout, charge dispersion gives better resolution for the GEM and the Micromegas.

# Charge dispersion TPC beam test in a magnet at KEK - October 2005

## Canada

A.Bellerive, K.Boudjemline, M.Dixit, J.Miyamoto,  
E.Neuheimer, E.Rollin, K.Sachs & Y.Shin  
J.-P. Martin

Carleton University

University of Montreal

## France

D.Burke, P.Colas, A.Giganon & I.Giomataris  
V.Lepeltier & Th.Zerguerras

DAPNIA CEA Saclay

LAL Orsay

## Germany

R. Settles

MPI (Munich)

## Japan

H.Kuroiwa & T.Takahashi  
K.Fujii, M.Kobayashi, T.Matsuda & H.Yamaoka  
Y.Kato  
T.Watanabe  
T.Araki, H.Fujishima, T.Higashi, , K.Kodomatsu,  
A.Sugiyama, T.Yamamoto & Y.Tanaka  
A.Yamaguchi  
M.Habu, S.Matsushita, K.Nakamura & O.Nito

Hiroshima University

KEK/IPNS

Kinki University

Kogakuin University

Saga University

Tsukuba University

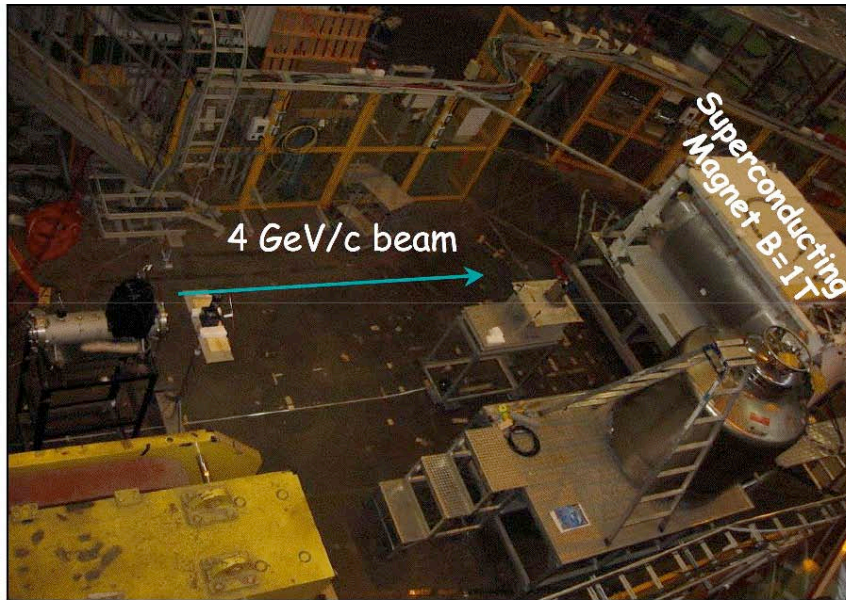
Tokyo University of

Agriculture & Technology

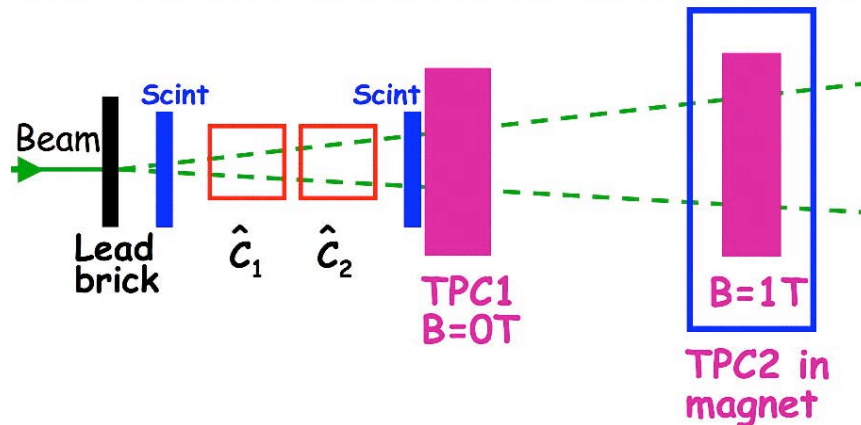


# KEK PS $\pi^2$ beam test of Carleton & MT3 TPCs

Beam data taken both in & outside the magnet for the two TPCs

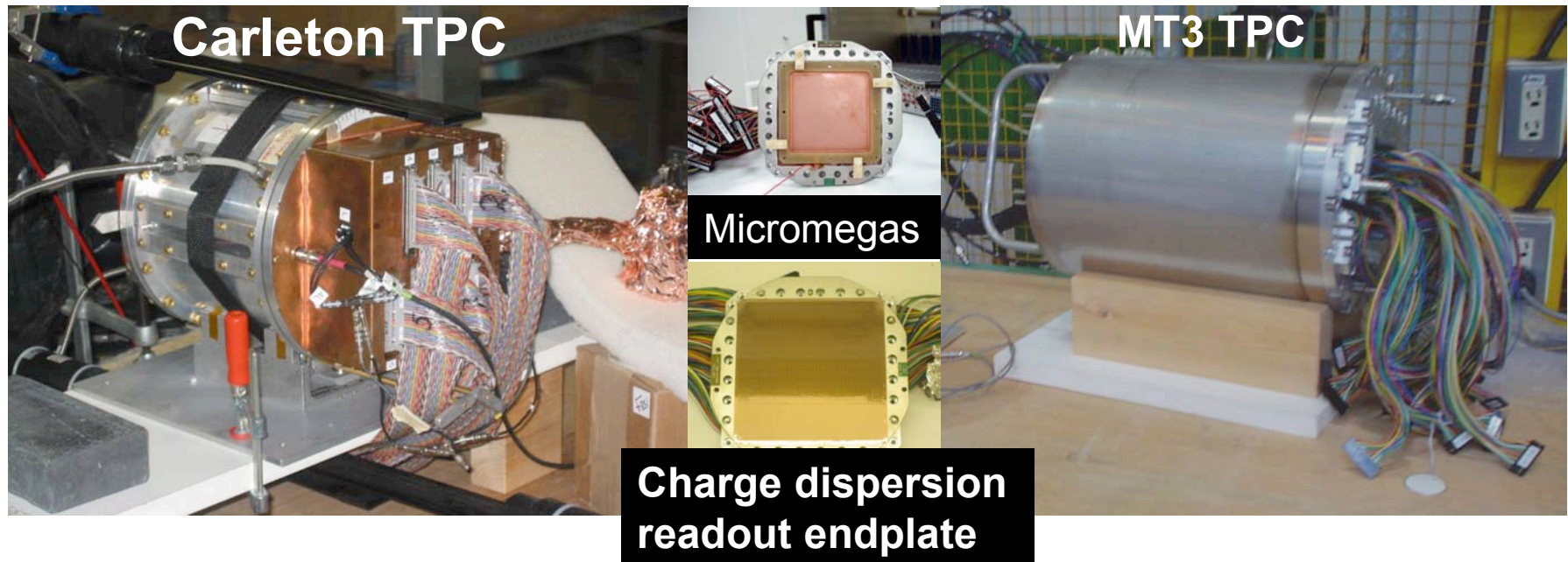


- 4 GeV/c hadrons (mostly  $\pi^{\pm}$ )
- 0.5 & 1 GeV/c electrons
- Super conducting 1.2 T magnet without return yoke
- Inner diameter : 850 mm
- Effective length: 1 m



**Carleton TPC in the beam outside the magnet**

## The two beam test TPCs



- Micromegas 10 x10 cm<sup>2</sup>
- Drift distance: 16 cm
- 126 pads, 2 x 6 mm<sup>2</sup> each in 7 rows
- ALEPH preamps + 200 MHz FADCs rebinned to 25 MHz equivalent FADCs

- Micromegas & GEMs 10 x10 cm<sup>2</sup>
- Drift distance 25.9 cm
- 384 pads 2.3 x 6.3 mm<sup>2</sup> each in 16 rows
- ALEPH preamps + 11 MHz Aleph Time Projection Digitizers

# Track display - Ar+5%iC4H10

## Micromegas 2 x 6 mm<sup>2</sup> pads B = 1 T

$Z_{\text{drift}} = 15.3 \text{ cm}$

Event Panel

### CARLETON-TPC TRACK DISPLAY

1 2 3 4 5 6 7 8 9 10

EXIT

File Edit View Options Inspect Classes Help

EXEC RESET

Event 9 Time = 1527 Z = 15.30 cm

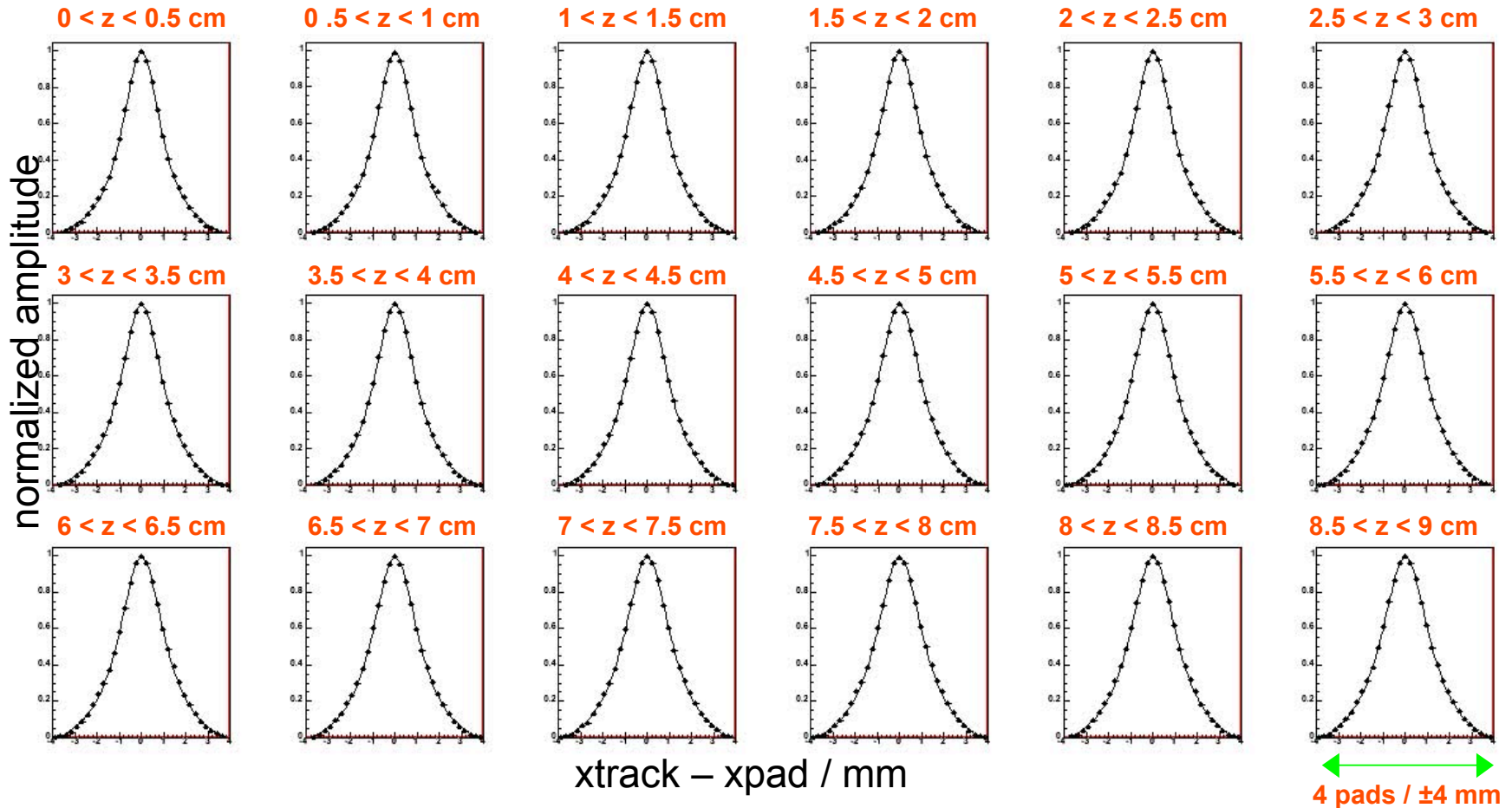
	18																>15%		
1	11	10	5	4	31	30	25	24	19	17	46	42	38	34	62	58	54	50	>13%
2	14	9	8	3	2	29	28	23	22	48	45	41	37	33	61	57	53	49	>11%
3	13	12	7	6	1	32	27	26	21	20	44	40	36	64	60	56	52	16	>9%
4	79	115	119	123	127	99	103	107	111	47	43	39	35	63	59	55	51	15	>7%
5	80	116	120	124	128	100	104	108	84	85	90	91	96	65	70	71	76	77	>5%
6	113	117	121	125	97	101	105	109	112	86	87	92	93	66	67	72	73	78	>3%
7	114	118	122	126	98	102	106	110	81	83	88	89	94	95	68	69	74	75	>1%
	82																>0%		

main pulse

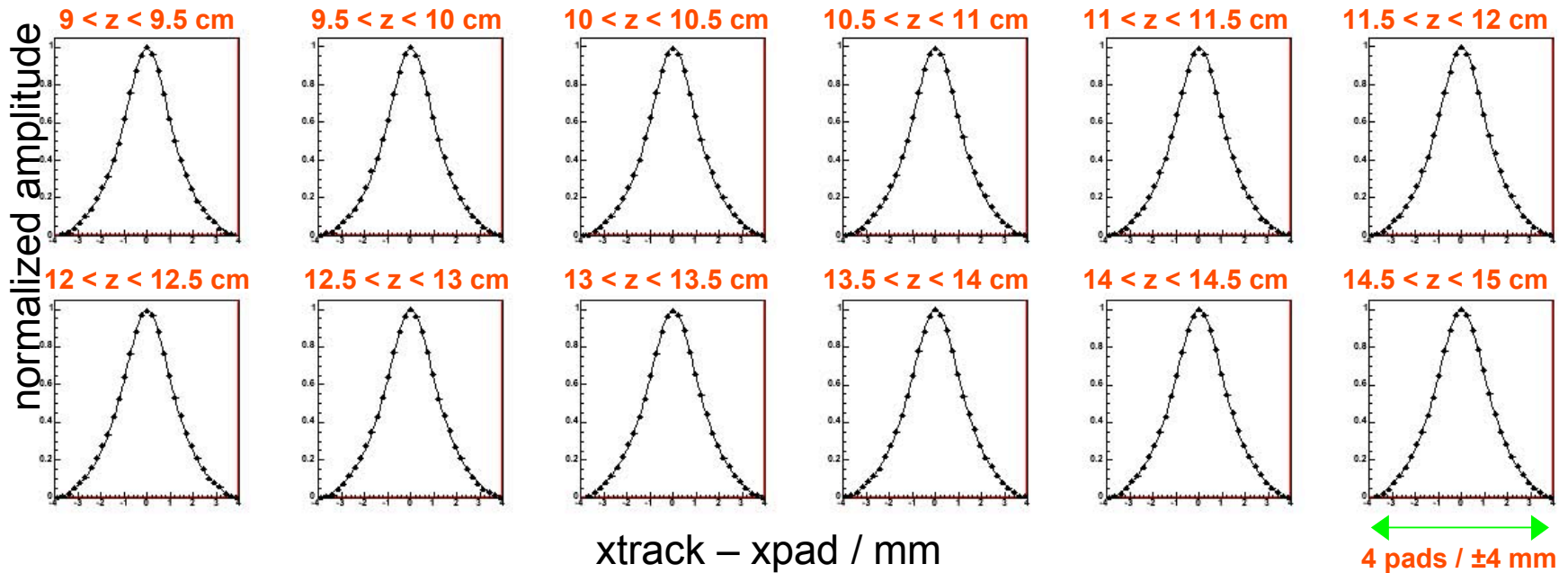
# Pad Response Function / Ar+5%iC4H10

## Micromegas+Carleton TPC 2 x 6 mm<sup>2</sup> pads, B = 1 T

30 z regions /  
0.5 cm step



# Pad Response Function / Ar+5%iC4H10



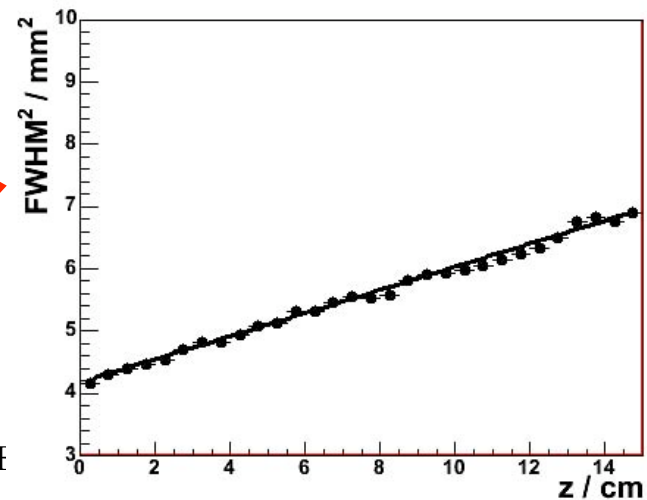
## PRF parameters

- $a = b = 0$
- $\Delta = \text{base width} = 7.3 \text{ mm}$
- $\Gamma = \text{FWHM} = f(z)$

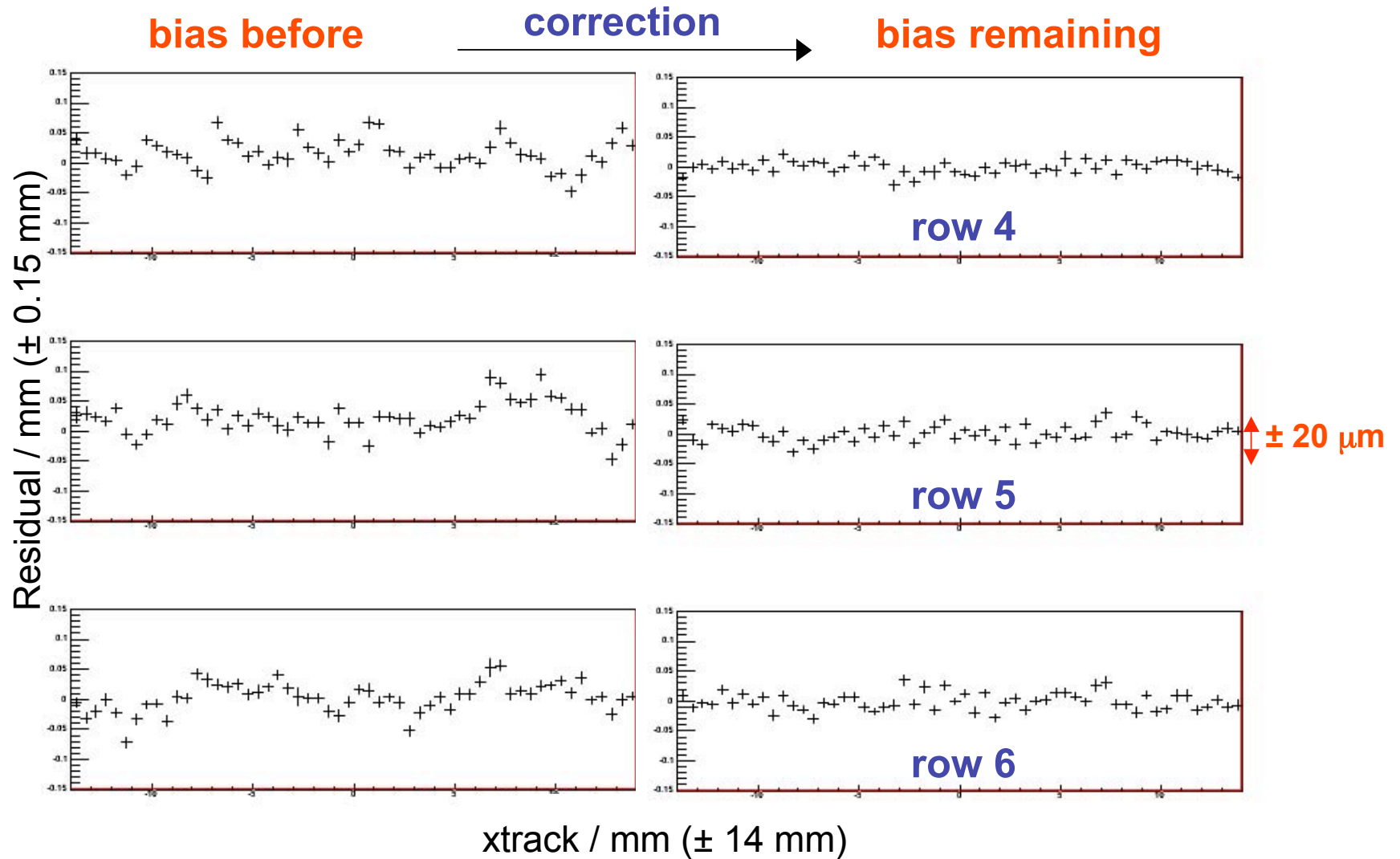
*The parameters depend on TPC gas & operational details*

7/4/2006

TPC Application Workshop - LI

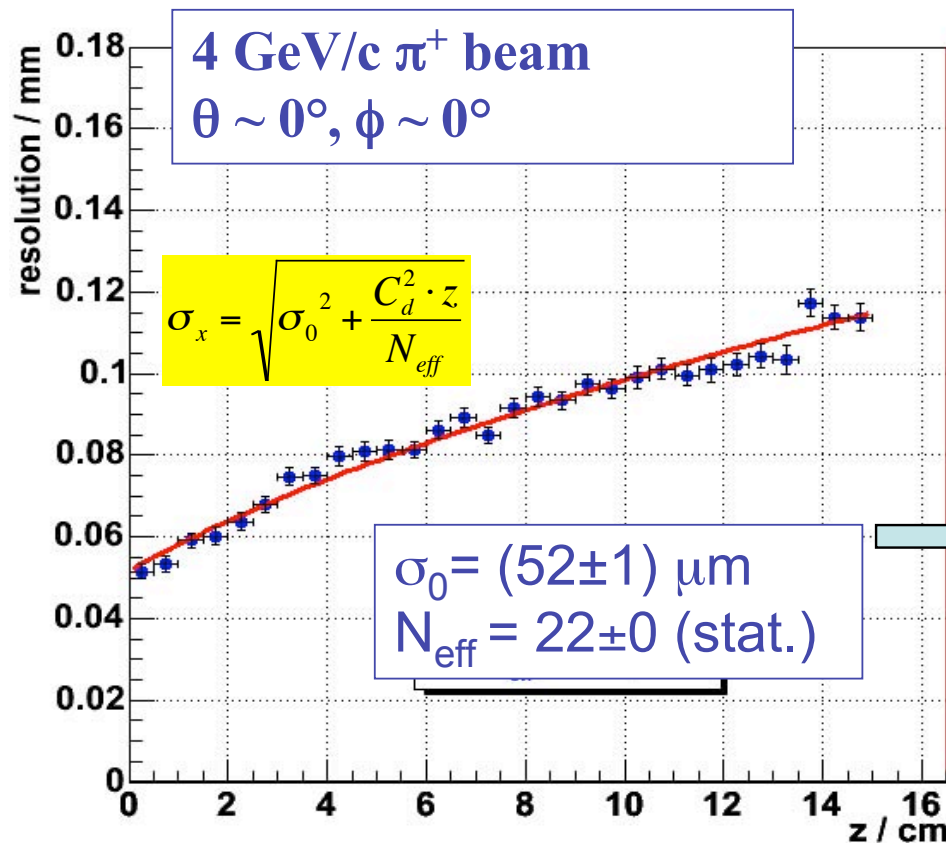


# Bias for central rows / Ar+5%iC4H10 B = 1 T



# Transverse spatial resolution Ar+5%iC4H10 E=70V/cm $D_{Tr} = 125 \mu\text{m}/\sqrt{\text{cm}}$ (Magboltz) @ B= 1T

## Micromegas+Carleton TPC 2 x 6 mm<sup>2</sup> pads



•Strong suppression of transverse diffusion at 4 T.

Examples:

$D_{Tr} \sim 25 \mu\text{m}/\sqrt{\text{cm}}$  (Ar/CH4 91/9)

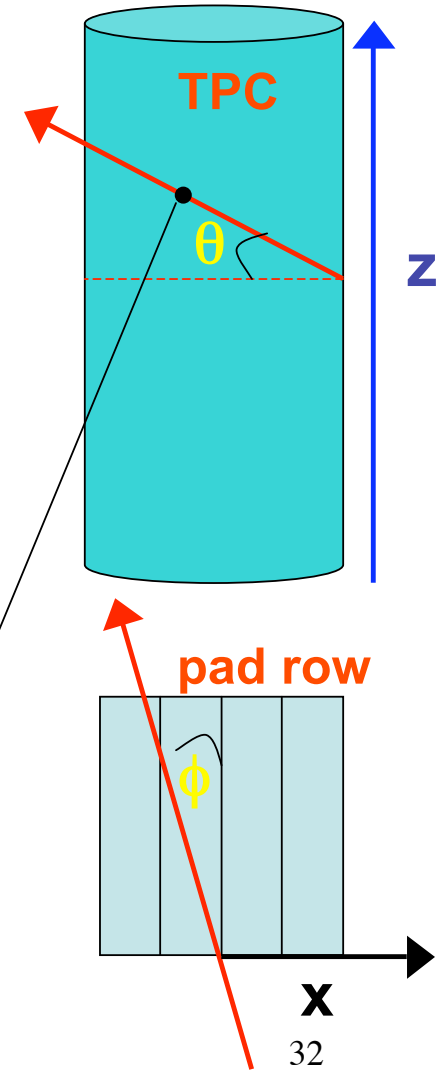
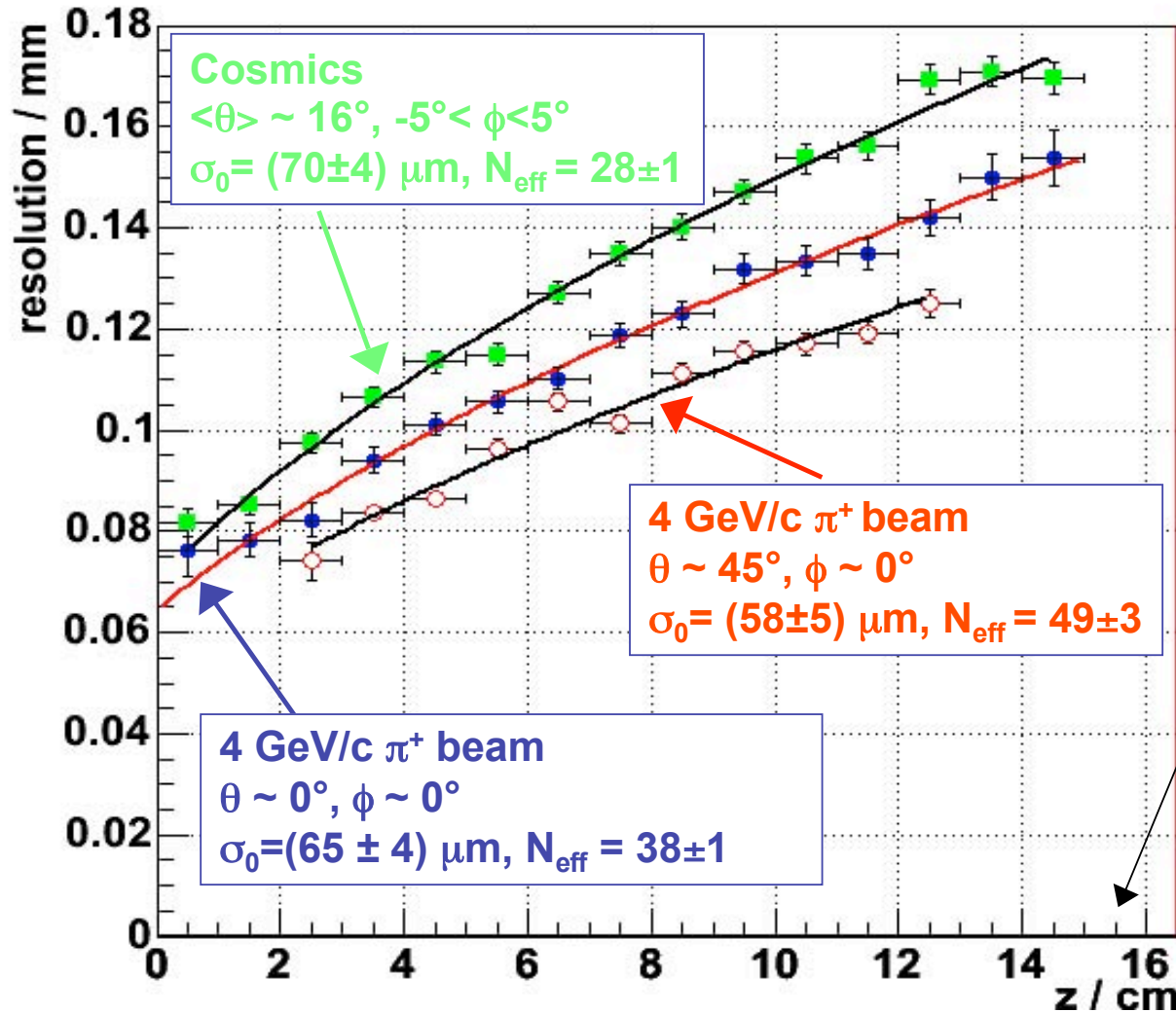
Aleph TPC gas

$\sim 20 \mu\text{m}/\sqrt{\text{cm}}$  (Ar/CF4 97/3)

**Extrapolate from present data to B = 4T**  
**Use  $D_{Tr} = 25 \mu\text{m}/\sqrt{\text{cm}}$**   
**Resolution (2x6 mm<sup>2</sup> pads)**  
 **$\sigma_{Tr} \approx 100 \mu\text{m}$  (2.5 m drift)**

Transverse resolution with no magnet - Angle dependence  
 Ar+10% CO<sub>2</sub>,  $D_{Tr} = 222 \mu\text{/}\sqrt{\text{cm}}$  (Magboltz)  $E=300 \text{ V/cm}$

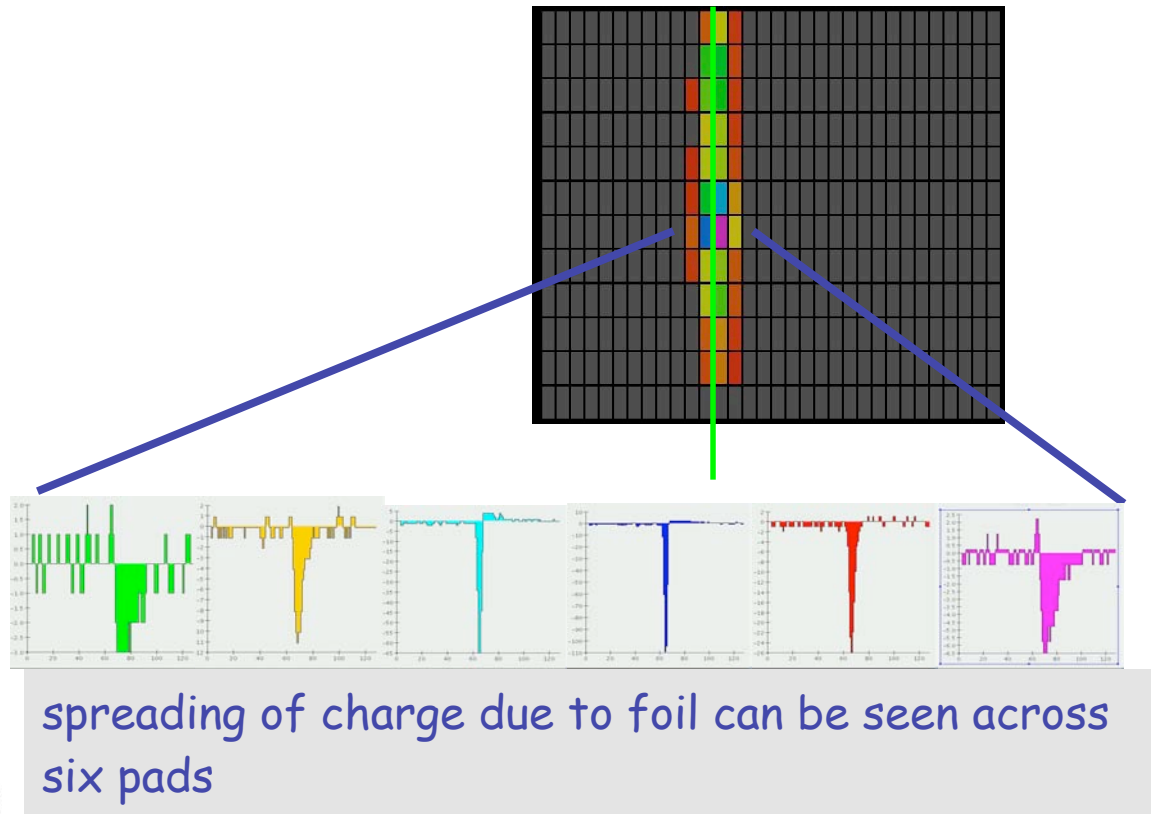
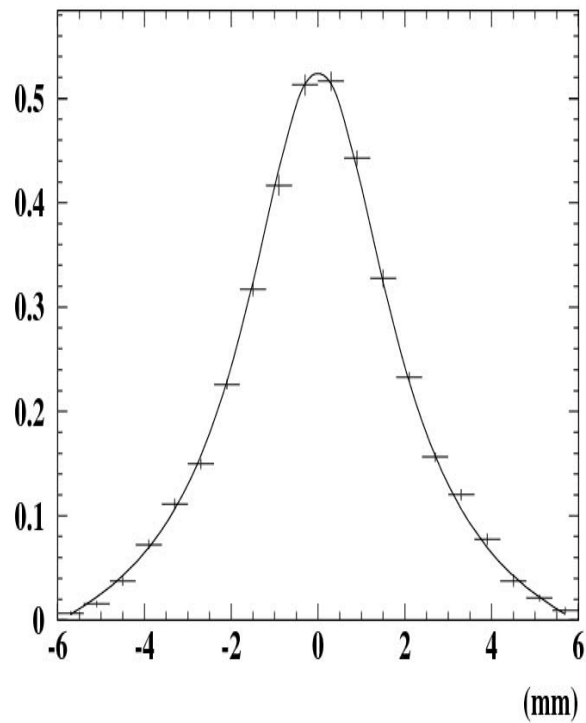
**Carleton TPC 2 x 6 mm<sup>2</sup> pads**





# MT3 TPC event display + Micromegas read out with Aleph TPDs 2.3 x 6.3 mm<sup>2</sup> pads Ar+5%iC4H10

$E=220\text{V/cm}$   $D_{Tr}=193\ \mu\text{m}/\sqrt{\text{cm}}$  @  $B=1\text{T}$

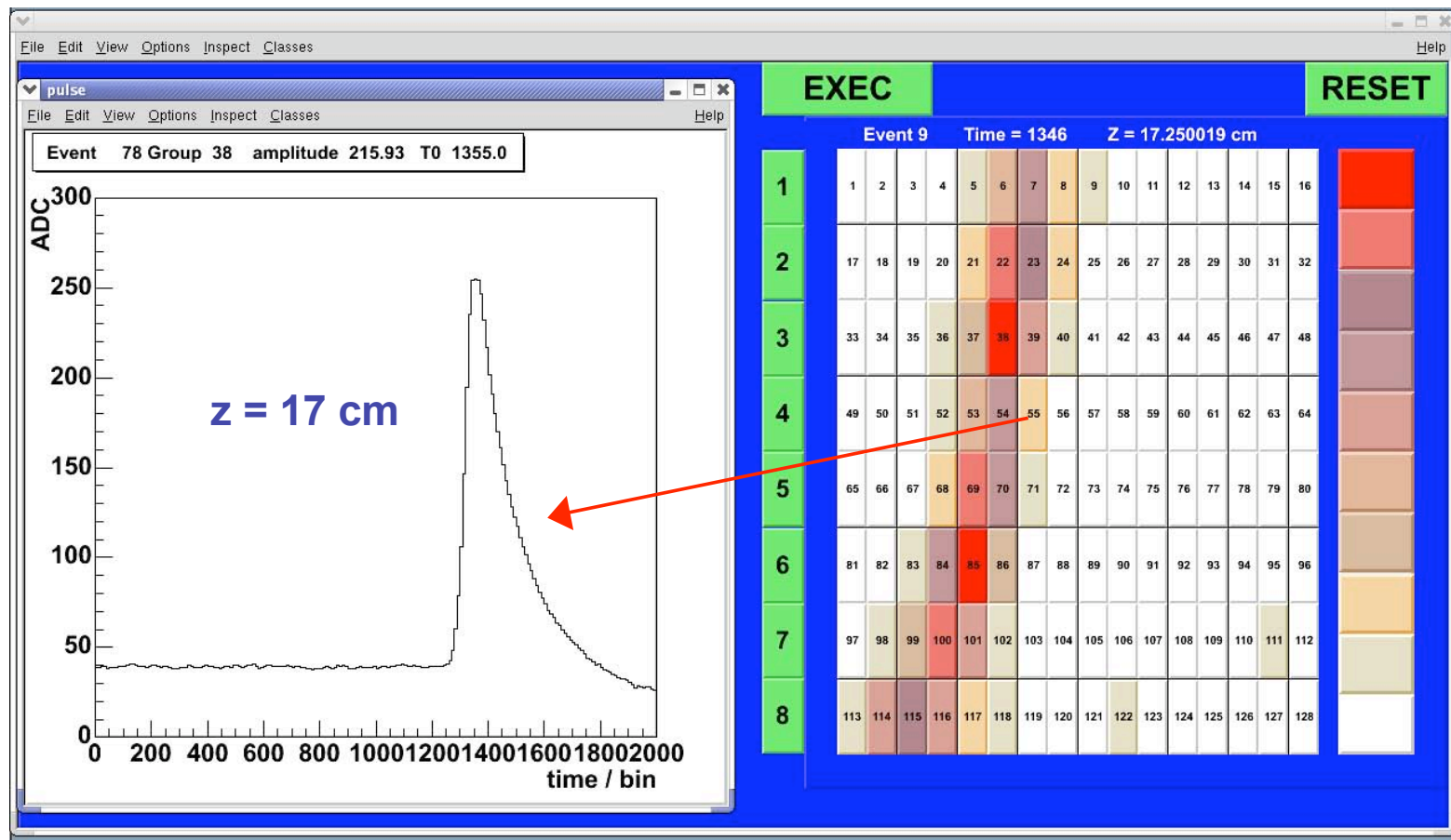


**Example pad response function**

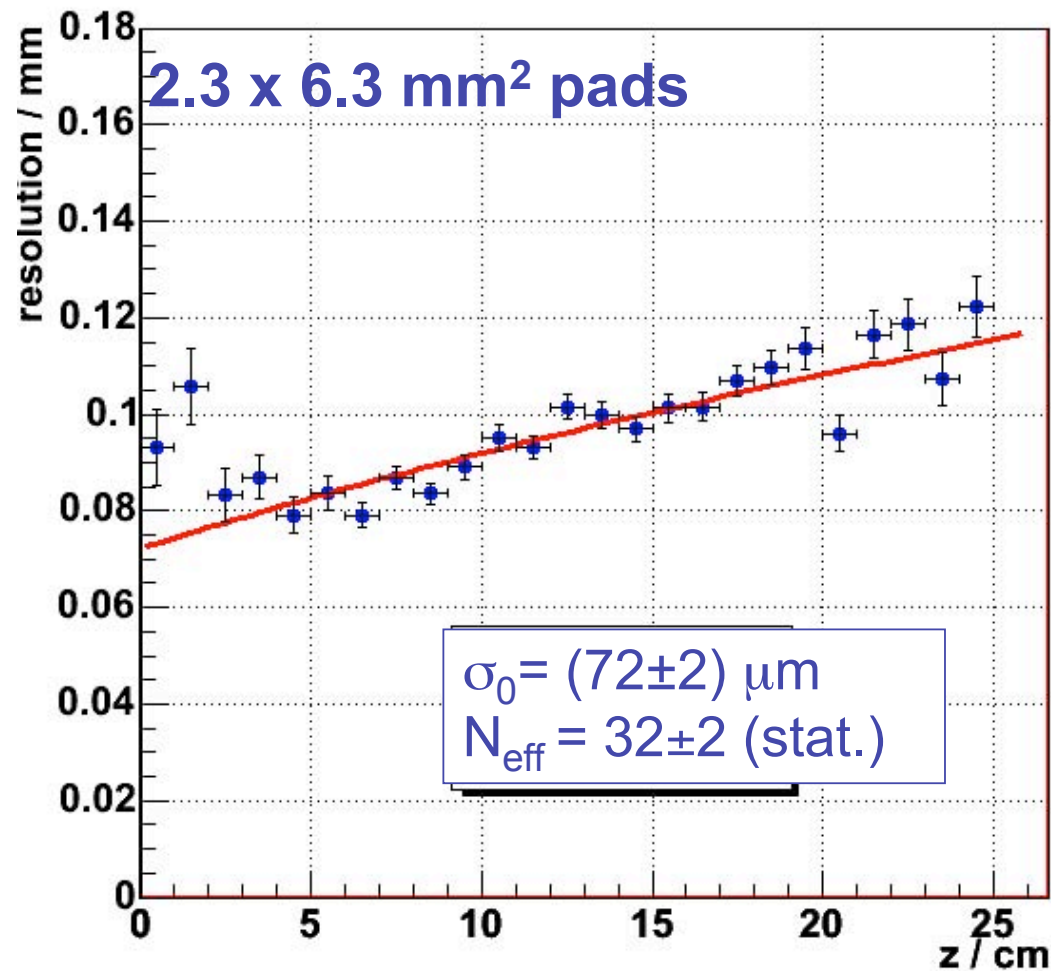
**Data analysis is in progress**

# Track display **MT3 TPC** with triple **GEM** readout

Part of **MT3-TPC** read out with **Carleton FADCs** 4 GeV/c  $\pi^+$  beam  
2.3 mm pitch x 6.3 mm pads 25 cm maximum drift distance  
**Ar/CH4 (95/5)**  $E = 50$  V/cm  $D_{Tr} = 102$   $\mu$ /v/cm (Magboltz) @ 1T

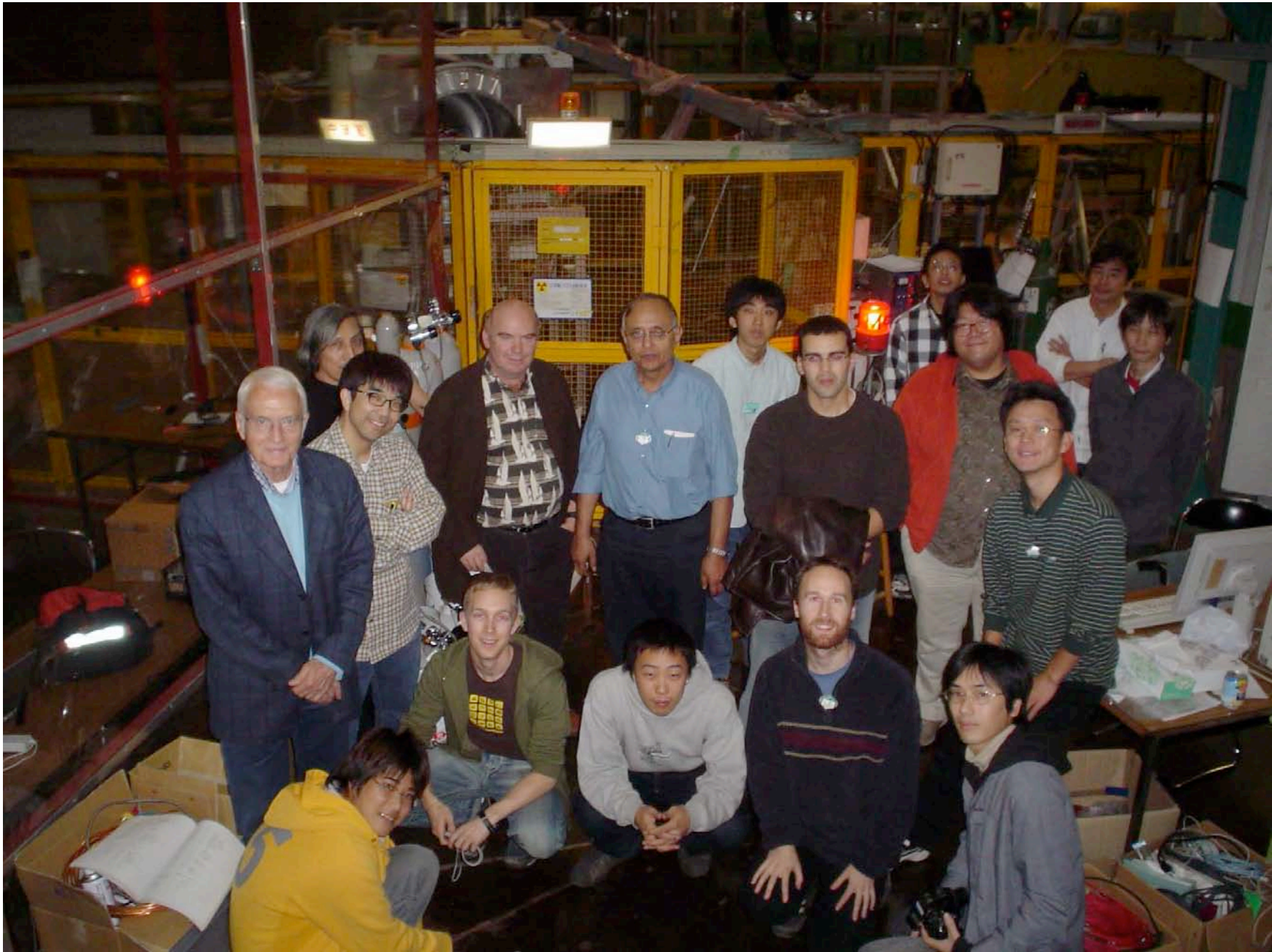


# Transverse resolution - **MT3-TPC with Triple GEM** Ar+5%CH4 E = 50 V/cm $D_{Tr} = 102 \mu\sqrt{\text{cm}}$ (Magboltz) @ 1T



## Summary

- Traditional MPGD-TPC readout has difficulty achieving good resolution if wide pads similar in width to conventional wire TPC pads are used.
- With charge dispersion, the cluster charge can be dispersed in a controlled way such that wide pads can be used without sacrificing resolution. With such a readout system, we have achieved excellent resolution with wide pads both for the GEM and the Micromegas.
- The ILC-TPC resolution goal, 100  $\mu\text{m}$  for all tracks, should be feasible with 2 x 6 mm<sup>2</sup> pads with a good understanding of systematics.
- R&D plans - cosmic ray TPC tests at 4 T & two track resolution studies in a beam.
- R&D issues: New technology issues of fabrication & quality control, understanding/reducing bias. As charge dispersion pulses are slow, ~25 MHz digitizers could be used.

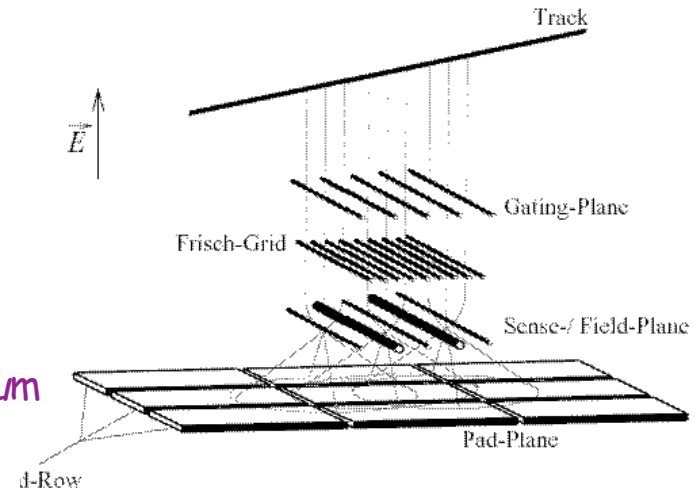
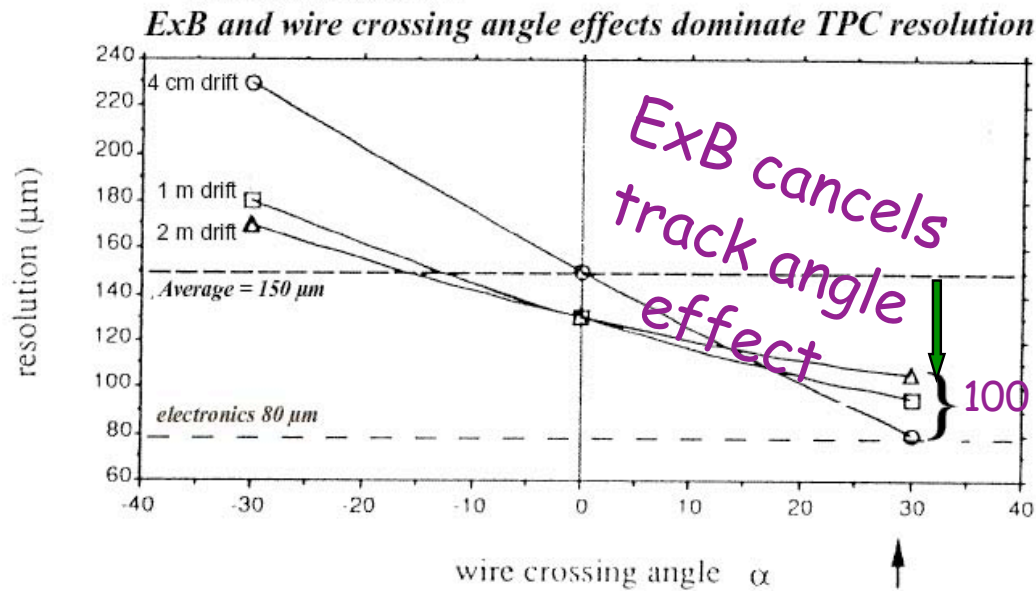


# Conventional TPCs never achieve their potential!

## Example: Systematic effects in Aleph TPC at LEP

S.R. Amendolia et al. / *The spatial resolution of the ALEPH TPC*  
 Nuclear Instruments and Methods in Physics Research A283 (1989) 573–577  
 North-Holland, Amsterdam

TPC wire/pad readout



- Average Aleph resolution  $\sim 150 \mu\text{m}$
- About  $100 \mu\text{m}$  best for all drift distances
- Limit from diffusion  $\sigma$  (10 cm drift)  $\sim 20 \mu\text{m}$ ;  $\sigma$  (2 m drift)  $\sim 90 \mu\text{m}$